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ABSTRACT

Structural Change out of Agriculture: Labor Push versus Labor Pull*

The process of economic development is characterized by substantial rural-urban migrations and a decreasing share of agriculture in output and employment. The literature highlights two main engines behind this process of structural change: (i) improvements in agricultural technology combined with the effect of Engel's law of demand push resources out of the agricultural sector (the "labor push" hypothesis), and (ii) improvements in industrial technology attract labor into this sector (the "labor pull" hypothesis). We present a simple model that features both channels and use it to explore their relative importance. We evaluate the U.S. time series since 1800 and a sample of 13 industrialized countries starting in the 19th century. Our results suggest that, on average, the "labor pull" channel dominates. This contrasts with popular modeling choices in the recent literature.

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“It is quite wrong to try founding a theory on observable magnitudes. . . It is the theory which decides what we should observe.” Albert Einstein, quoted by Heisenberg (1972, p. 63).

1 Introduction

The process of economic development is always and everywhere characterized by substantial reallocations of resources out of agriculture. While most economists agree that this structural transformation has been driven by productivity increases, there is no consensus on whether technological progress in manufacturing or in agriculture has been more important. Yet, given the continuing importance of the agricultural sector in today’s poor economies, it is crucial to have a proper understanding of the historical determinants of structural change. To address this, we propose a simple model that encompasses both sources of structural change to show how to identify their relative importance in the data. We use this model to explore the historical experience of 13 countries that have completed their process of structural reallocation, using data from the 19th century onwards.¹

Already Clark (1940), Kuznets (1966) and Chenery and Syrquin (1975) documented the process of structural transformation: the fall in the share of agriculture in output and employment that accompanied long-run increases in income per capita. As an example, in 1800, the U.S. economy employed around three fourths of its labor force in the agricultural sector. The sector accounted for more than half of total output. Two hundred years later, only 2.5% of the labor force remained in the agricultural sector and the share of agricultural production in GDP was below 1%. Over these two centuries, U.S. output per capita increased more than 25 times.

Although development economists and economic historians have long been interested in this process of structural transformation, there has been and still is substantial debate about the relative roles technological progress in the agricultural and the manufacturing sectors played in the process, with classical and more recent contributions on both sides.

On the one hand, there is a continuing tradition that places the emphasis of the transformation on the manufacturing sector. Lewis (1954) presents a model where capital accumulation in the modern sector raises urban wages and attracts surplus labor from the

¹In this paper, we use the term “structural change” in a narrow sense to refer exclusively to movements of resources out of the agricultural sector. Moreover, to keep the prose simple, we will use the terms “modern sector” and “manufacturing sector” to refer to the entire non-agricultural sector.

agricultural sector. Reinvestment of profits keeps the process going. Similarly, Harris and Todaro (1970) present a two sector model in which rural-urban migration results from positive differences between the expected urban (industrial) real income and agricultural product per worker. Both theories suggest that technological progress and investment in manufacturing raise urban incomes and drive the process of structural change. In this view, increasing industrial wages attract low-paid or underemployed labor from agriculture into manufacturing. Following Gylfason and Zoega (2006) we refer to this as the “labor pull” hypothesis. Hansen and Prescott (2002) model a similar mechanism and conclude that “the (modern) technology must improve sufficiently so that it ultimately becomes profitable to shift resources into this sector”.

On the other hand, some scholars consider agricultural productivity the main driver of structural change. Nurkse (1953) argues that “everyone knows that the spectacular industrial revolution would not have been possible without the agricultural revolution that preceded it”. Rostow (1960) identifies increases in agricultural productivity as a necessary condition for a successful take-off. These authors suggest that improvements in agricultural technology allow solving the “food problem” (Schultz 1953), so that resources can be released from the agricultural to the manufacturing sector. We refer to this as the “labor push” hypothesis. Recently, Gollin, Parente and Rogerson (2002, 2007) provide a modern formalization of these ideas. In their words, “improvements in agricultural productivity can hasten the start of industrialization and, hence, have large effects on a country’s relative income. A key implication of the model is that growth in agricultural productivity is central to development.” Productivity growth in agriculture also acts as the main driver of the structural transformation in Ngai and Pissarides (2007).

Our objective is to provide empirical evidence on the relative importance of the “push” and “pull” hypotheses. We present a simple model close to Matsuyama (1992) and to Kongsamut, Rebelo and Xie (2001) that is consistent with the two crucial observations associated with the process of structural change: a secular decline in the share of the labor force devoted to agriculture and a decreasing weight of agricultural output in national product. Our model captures both sources of structural change highlighted in the literature: improvements in agricultural technology combined with Engel’s law of demand shift resources to the industrial sector, and improvements in manufacturing technology increase manufacturing wages, pulling labor into that sector. We use this framework to assess the effects of increases in agricultural and manufacturing productivity on key

observable variables. Both hypotheses lead to qualitatively similar behavior of labor allocations, the share of agriculture in GDP, and wages. They differ in their predictions for the evolution of the relative price of manufactures relative to agricultural goods. Hence, data on the relative price allow identifying which sector is the main engine of the structural transformation. In this sense, our exercise follows a long tradition in economics that uses changes in relative prices to infer changes in productivity. A recent example is Greenwood, Hercowitz and Krusell (1997).

We then explore the determinants of structural change using data on relative prices and on agricultural labor shares in two samples: the U.S. time series since 1800 and a long panel of 13 industrialized countries starting in the 19th century. Since for the U.S., estimates of sectoral productivities are available, the first exercise allows us to confirm the validity of our basic identifying strategy. In line with the model predictions, the relative price is almost a mirror image of relative productivity. For the larger sample, not all of the data required to compute sectoral productivities is available. In these circumstances, our parsimonious approach that relies on the relative price provides important insights that could not be obtained otherwise.

There are three main findings. Firstly, there is a lot of heterogeneity; both channels play a role. For instance, in the case of the U.S. it is very clear that the “labor pull” channel dominated before World War I, with the “labor push” channel taking over after World War II (this period has also been dubbed the Green Revolution). Secondly, on average, increases in non-agricultural productivity slightly outpaced those in agricultural productivity, pointing to the “labor pull” channel as a somewhat more important driver of structural change overall. Finally, we find that the decline in the agricultural labor share is larger when the productivity of manufacturing increases relative to that of agriculture than the other way round. This holds at all stages of the structural transformation.

The main contribution of our paper hence is to provide insights about the historically important drivers of structural change. Our results have important implications for modeling that process. In particular, models of structural change that rely on faster productivity growth in agriculture such as Ngai and Pissarides (2007) seem to be at odds with most of the the pre-World War II evidence. Moreover, models of structural change that restrict non-homotheticities in preferences to food consumption, such as Gollin, Parente and Rogerson (2002), seem to miss non-agricultural technological progress as an important driver of structural change. As a consequence, our results cast some doubt on some of

the estimates and policy recommendations derived using modeling strategies that neglect the crucial role played by non-agricultural productivity in the process of structural change and economic development. Given the continuing importance of the agricultural sector in today's poor economies and its impact on aggregate productivity differences documented by Caselli (2005), Temple and Woessmann (2006) and Restuccia, Yang and Zhu (2008), among others, it is crucial to have a proper understanding of the historical determinants of structural change.

The paper is organized as follows. Section 2 sets out the basic model and explores the implications of increases in agricultural and manufacturing productivity. Section 3 evaluates our model against the U.S. experience. Section 4 explores the determinants of structural change in a long panel of 13 industrialized countries. The conclusions are summarized in Section 5, while the Appendices provide some technical details and data descriptions.

2 Agricultural Push vs. Industrial Pull in a simple model of structural change

We consider a closed economy that consists of two sectors: a traditional sector devoted to the production of agricultural goods and a modern sector that produces industrial commodities and services. The size of the labor force is constant and normalized to 1. Both production technologies exhibit weakly diminishing returns to labor,

$$\begin{aligned} Y_t^M &= MF(L_t^M), & M > 0, F' > 0, F'' \leq 0 \\ Y_t^A &= AG(L_t^A), & A > 0, G' > 0, G'' \leq 0, \end{aligned}$$

where L_t^M and $L_t^A = 1 - L_t^M$ are the amounts of labor employed in manufacturing and in agriculture respectively, and M and A denote the levels of technology in the two sectors. For the moment, we assume that both technology parameters are constant.

As in Matsuyama (1992), labor can move freely across sectors. Then, competition

between firms in both sectors ensures that a non-arbitrage condition holds:²

$$w_t^A = AG'(1 - L_t^M) = p_t MF'(L_t^M) = w_t^M,$$

where w_t^A is the real wage in the traditional sector and w_t^M that in the modern sector. p_t is the relative price of the manufacturing good which can be expressed as

$$p_t = \frac{AG'(1 - L_t^M)}{MF'(L_t^M)}. \quad (1)$$

Consumers are identical, infinitely lived, and inelastically supply their labor endowment. Their preferences are given by

$$U(c_t^A, c_t^M) = \alpha \ln(c_t^A - \gamma) + \ln(c_t^M + \mu), \quad \alpha, \gamma, \mu > 0, \quad (2)$$

where c_t^A and c_t^M denote individual consumption of food and manufactures, respectively, and α the relative weight of food in preferences. These preferences are non-homothetic for two reasons. First, we introduce a subsistence level of food consumption, γ . As a result, the income elasticity of food demand is below one, in line with the evidence on the universality of Engel's law known at least since Houthakker (1957). This feature of preferences has long been emphasized in the literature on sectoral reallocation (Matsuyama 1992, Laitner 2000, Caselli and Coleman 2001, Gollin et al. 2002). Second, we assume that the income elasticity of non-agricultural goods is greater than one. Following Kongsamut et al. (2001) we can interpret μ as an exogenous endowment of non-agricultural goods, possibly resulting from home production.³ Finally, we assume that the level of agricultural productivity is high enough so that our economy operates above the subsistence level of food,

$$AG(1) > \gamma. \quad (3)$$

²The extent of integration of the rural labor market with the rest of the economy is a topic of debate. While some development economists argue that it is low, Magnac and Postel-Vinay (1997) provide evidence from 19th century France that "migration between industry and agriculture was quite sensitive to relative wages in the two sectors" and that firms took this into account in their decisions. They also find that wages were similar in the two sectors. Moreover, our qualitative results are robust to the introduction of quadratic migration costs à la Krugman (1991).

³For instance, clothes can be washed using a washing machine (a component of c_M) or by hand (home production). Our specification can thus be interpreted as modeling home production in reduced form, similar to Kongsamut et al. (2001) and Duarte and Restuccia (2010). In Appendix A, we introduce a generalized CES specification that yields identical results when $\mu = 0$. Nonetheless we believe that our exposition is clearer under (2).

The representative household chooses his consumption bundle to maximize the present value of (2), discounted at a rate $\rho > 0$, subject to the budget constraint

$$w_t^A(1 - l_t^M) + w_t^M l_t^M = c_t^A + p_t c_t^M, \quad (4)$$

where l_t^M represents time spent working in the modern sector.⁴ Together with (4), the optimality conditions associated with this program are

$$\begin{aligned} \frac{\alpha}{c_t^A - \gamma} &= \lambda \\ \frac{1}{c_t^M + \mu} &= \lambda p_t, \end{aligned}$$

where λ is the shadow value of an additional unit of income. Optimizing households equate the marginal rate of substitution between the two consumption goods to the relative price. Combining these two equations, the individual demand for the agricultural good satisfies $c_t^A = \gamma + \alpha p_t (c_t^M + \mu)$. Aggregating across households and using upper case letters for aggregate variables, this becomes

$$C_t^A = \gamma + \alpha p_t (C_t^M + \mu). \quad (5)$$

In equilibrium, all output from both sectors is consumed, so $C_t^A = Y_t^A$ and $C_t^M = Y_t^M$. Combining the market clearing condition with (1) and (5) yields the following relation for the allocation of labor between sectors.

$$\frac{\gamma}{A} = G(1 - L_t^M) - \alpha \frac{G'(1 - L_t^M)}{F'(L_t^M)} \left(F(L_t^M) + \frac{\mu}{M} \right) = \phi(L_t^M, M) \quad (6)$$

where

$$\phi(L_t^M, \bar{M}) < \phi(0, \bar{M}) = G(1); \quad \phi_{L_t^M} < 0; \quad \phi_M > 0,$$

where ϕ_x denotes the partial derivative of ϕ with respect to the variable x . Given (3), equation (6) has a unique solution that determines the level of employment in the non-agricultural sector.

To obtain the effect of productivity increases on the sectoral allocation, differentiate (6) with respect to the productivity parameters:

$$\frac{\partial L^{M*}}{\partial A} = -\frac{\gamma}{A^2 \phi_{LM}^*} > 0 \quad (7)$$

$$\frac{\partial L^{M*}}{\partial M} = -\frac{\phi_M^*}{\phi_{LM}^*} > 0, \quad (8)$$

⁴Since we abstract from capital accumulation, our problem is simply a sequence of static problems.

where equilibrium choices are denoted by *. Productivity increases in either sector lead to flows of labor out of agriculture. Our model thus captures the two engines behind the large reallocation of labor out of agriculture that were highlighted in the introduction. As in Matsuyama (1992) and Gollin et al. (2002), increases in the level of agricultural productivity push labor out of the agricultural sector: the “labor push” effect discussed by Nurkse (1953) and Rostow (1960). But additionally, as in Hansen and Prescott (2002), improvements in the level of technology in the industrial sector pull labor out of the traditional sector, increasing manufacturing employment: the “labor pull” effect stressed by Lewis (1954) and Harris and Todaro (1970). The income elasticities of demand for agricultural and non-agricultural commodities lie behind these two effects. Notice that if $\gamma = 0$ the labor allocation is independent of the level of agricultural technology and if $\mu = 0$ the labor allocation is independent of the level of technology in the non-agricultural sector.

Our model is also consistent with the second stylized fact of structural change, the secular decline of the share of agriculture in GDP. Consider the ratio of non-agricultural to agricultural output,

$$\frac{p_t Y_t^M}{Y_t^A} = \frac{G'(1 - L_t^M)}{F'(L_t^M)} \frac{F(L_t^M)}{G(1 - L_t^M)}.$$

This expression increases in L_t^M , the share of labor employed in non-agricultural production. Hence, increases in productivity in either sector reduce the share of agriculture not only in employment but also in output.

Finally, we can evaluate the effects of technological change on the relative price of manufactures. Using (1), (5), (7) and (8), we find the following comparative statics results for the relative price,

$$\frac{\partial p^*}{\partial A} = \frac{\left[G'(\cdot) - AG''(\cdot) \frac{\partial L^{M^*}}{\partial A} \right] F'(\cdot) - AG'(\cdot) F''(\cdot) \frac{\partial L^{M^*}}{\partial A}}{M [F'(\cdot)]^2} > 0$$

$$\frac{\partial p^*}{\partial M} = -\frac{AG'(\cdot) \frac{\partial L^{M^*}}{\partial M}}{\alpha [MF(\cdot) + \mu]} - \frac{(AG'(\cdot) - \gamma) \left(F(\cdot) + MF'(\cdot) \frac{\partial L^{M^*}}{\partial M} \right)}{\alpha [MF(\cdot) + \mu]^2} < 0.$$

We can use this simple framework with only labor and costless reallocation between sectors to explore the empirical implications of the labor-push and labor-pull hypotheses. Both hypotheses are associated with migrations from the countryside to the manufacturing

centers and with a declining weight of agriculture in national product. Furthermore, both hypotheses are associated with increases in rural and urban wages. But while increases in agricultural productivity, A , are associated with increases in the relative price of the non-agricultural good, increases in the level of productivity in the modern sector, M , reduce the relative price of non-agricultural goods. Thus, while the evolution of wages, labor allocations or sector output shares provides little information to discriminate between the two hypotheses, the behavior of relative prices gives crucial insights about the relative roles of the agricultural revolution and the industrial revolution in the process of structural change that started in Britain more than two centuries ago. In this sense, our exercise follows a long tradition in economics that uses changes in relative prices to infer changes in productivity. A recent example is Greenwood et al. (1997).

Finally, we turn to explore the implications of our model in the presence of continuous technological change in both sectors, most likely the empirically relevant case. Denoting the instantaneous growth rates of agricultural and non-agricultural productivity by $\hat{A} > 0$ and $\hat{M} > 0$, respectively, and denoting the change in the share of labor in manufactures by \dot{L}^M , we use (1) to reach the following expression for the growth rate of the relative price.

$$\hat{p} = \hat{A} - \hat{M} - \dot{L}^M \left[\frac{G''(1 - L_t^M)}{G'(1 - L_t^M)} + \frac{F''(L_t^M)}{F'(L_t^M)} \right] > \hat{A} - \hat{M} \quad (9)$$

As long as there is no technological regress, the last inequality holds. This inequality implies that decreases in the relative price of manufactures are unambiguously associated with faster technological change in the non-agricultural sector, i.e. they indicate that the “labor pull” effect dominates. If the relative price rises, the situation is less clear. An equal increase in both sectors’ productivities induces an increase in the relative price of manufactures, resulting from the low income elasticity of demand for food and the high income elasticity of demand for manufactures. So only a strong increase in the relative price is a sign of stronger growth in agricultural productivity, or “labor push”. A weak increase in the relative price can well occur in a situation where the productivity in manufacturing has increased by slightly more.⁵

⁵Finally, it is worth noticing that in the presence of international trade, the labor allocation decision is independent of the consumption decision. A small open economy takes the relative price as given and, assuming that labor is mobile across sectors but immobile across countries, the domestic labor allocation is uniquely determined by (1). Given the world relative price, an increase in agricultural productivity then induces a shift of resources to agriculture, the now more productive sector. Increases in manufacturing productivity “pull” labor out of the agricultural sector leading to similar but more intense

In the next two sections, we exploit the implications of our model to explore the sources of structural change using two centuries of U.S. data and a long panel of 13 countries that already completed the process of structural transformation.

3 A long-term view of structural change in the U.S.

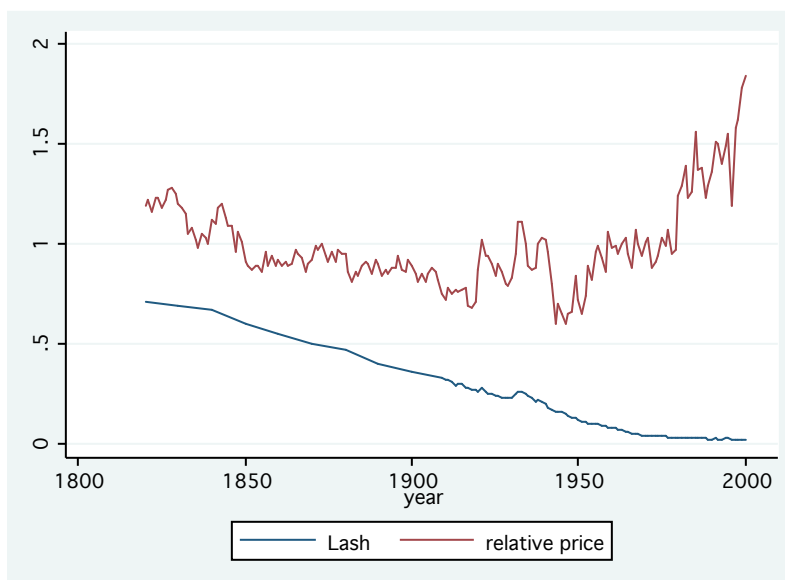
Although large migrations out of the agriculture began in the UK more than two centuries ago, the U.S. was one of the first countries to complete this process of structural transformation. Furthermore, the wealth and quality of the U.S. data, which besides relative prices includes data on sectoral productivities, makes this country an ideal candidate to evaluate the basic prediction of our model that changes in the relative price reflect changes in relative productivity. In particular, equation (9) implies that if the relative price falls, it must be that productivity in the non-agricultural sector has increased at a faster pace than agricultural productivity.

Figure 1 presents the evolution of the share of employment in agriculture and the relative price of manufactures to agricultural goods for the U.S. from 1800 to 2000. Over these two centuries, the share of labor employed in agriculture declined from 73% to barely 2.5%. This decline was monotonic, except for the period of the Great Depression.⁶ In contrast, the relative price declined steadily until 1918, then became more volatile until the end of World War II, after which it went on an upward trend. Our model then identifies a change in the main driver behind the process of structural transformation after World War II: the labor pull effect dominates before the war, with the labor push effect taking over later on. This implies that non-agricultural productivity growth outpaced its agricultural counterpart from the beginning of our sample period to World War I, with roles reversing after World War II.

This prediction is consistent with existing estimates of farm and non-farm productivity migrations than in the closed economy scenario. See Matsuyama (1992, 2009) for specific details on the open economy scenario. However, footnote 10 provides evidence that the closed economy assumption seems more appropriate for our sample.

⁶Only recently have real business cycles scholars made an attempt to explain the Great Depression in terms of fully specified stochastic general equilibrium models, see Prescott (1999) and Cole and Ohanian (1999, 2002). Their estimates suggest a 14% drop in TFP between 1929 and 1934. In the context of the model outlined in the previous section, a drop in TFP in any sector will trigger a process of reverse migration similar to the one observed in the data.

Figure 1: The share of employment in agricultural and the relative price of manufactures to agricultural goods, U.S., 1820-2000

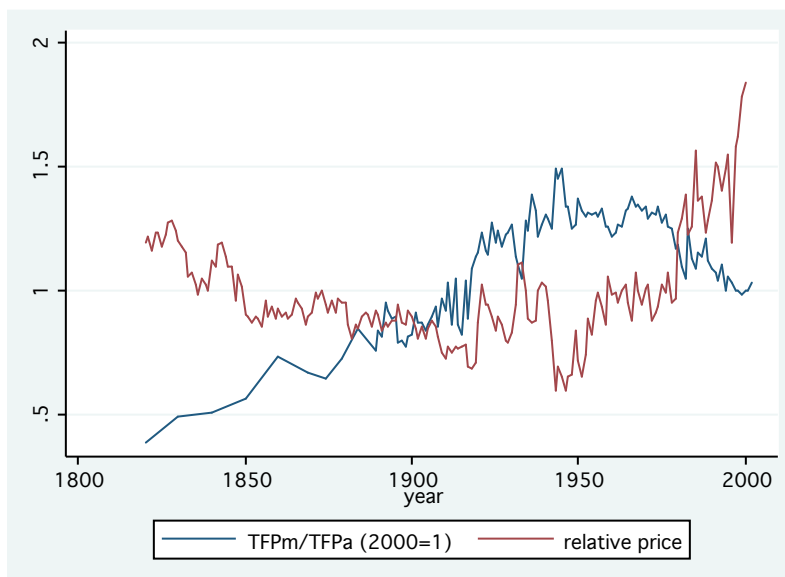


Sources: See Table 5.

in the U.S..⁷ Figure 2 plots the relative price of manufactures to agricultural goods and the relative productivity in the two sectors. Productivity is almost a mirror image of the price. In particular, it is striking to see that while the average growth rate in the non-farm sector outstrips that in the farm sector by 1% over the period from 1820 to 1948, the trend strongly reverses for the 1948 to 2002 period: in the second half of the twentieth century, average yearly TFP growth in the non-farm sector is 1.4%, compared to 1.7% in the farm sector. Not surprisingly this latter period, characterized by the rapid adoption of new agricultural technologies, has been known as the “Green Revolution”. For instance, after World War II, the adoption rates of tractors and of hybrid corn increased rapidly (Griliches 1957, Olmstead and Rhode 2001), contributing to rapid productivity growth in agriculture. More importantly, the results of this comparison are consistent with the basic prediction of our model and give us confidence to extend our identification strategy based on relative price data to a larger sample of countries where data on sectoral productivity is not readily available.

⁷See notes to the figure for sources.

Figure 2: Relative productivity (2000=1) and relative price of non-farm and farm goods, U.S., 1820-2000



Sources: U.S. farm productivity is from Gallman (1972, Table 7) for 1800-1840, from Craig and Weiss (2000, Table 3) for 1840-1870 (both cited in Dennis and Iscan 2009), from Kendrick (1961, Table B-I) for 1869-1948, and from the United States Department of Agriculture (USDA) Economic Research Service, Agricultural Productivity Data Set, <http://www.ers.usda.gov/Data/AgProductivity/>, for 1948-2000. Non-farm productivity is from Sokoloff (1986, Table 13.9) for 1820-1860 (again cited in Dennis and Iscan 2009), from Kendrick (1961, Table A-XXIII) for 1870-1948, and from the Bureau of Labor Statistics (BLS) Multifactor Productivity Trends – Historical SIC Measures 1948-2002, <http://www.bls.gov/mfp/historicalsic.htm>, for 1948-2000.

4 Historical evidence from some successful transformers

Is the U.S. experience representative? To answer this question, we gather data on labor allocations and relative prices for a sample of 13 countries that have completed their process of sectoral reallocation by the end of the twentieth century. Besides this, data availability determines whether a country is included in our sample.

In contrast to the use of relative productivity series, the use of the relative price has several advantages in terms of data requirements and functional form restrictions. First, the relative price strategy is less demanding in terms of data, giving us more and longer

series to work with. Computing TFP is a data intensive exercise that, besides the data on labor allocations and prices that we use, requires data on output, other inputs and factor shares. In most cases, these other series are not available. They are also harder to measure and therefore likely less reliable than the data we use. Second, by using relative prices we avoid imposing the stronger restrictions on the production function required to obtain TFP estimates. Finally, our empirical exercise will go beyond the simple inspection of the evolution of the relative price and will attempt to explore the extent to which the labor reallocation responds to changes in relative price to uncover the relative importance of labor push and labor pull in the process of structural change.

4.1 Data sources and overview

Our sample consists of 13 countries that have completed the process of structural transformation by the end of the twentieth century and for which we have data on labor allocations and relative prices. For many of these countries, data is available starting in the 19th century. While the number of countries in our sample is not large, the series cover a long span of time, giving a complete picture of the process of structural transformation in these countries. Details on coverage and sources are summarized in Tables 5 and 6 in Appendix B. To abstract from short-run fluctuations and to make figures comparable across data sources, we use five-year moving averages of both variables where data is available at a higher frequency.⁸

Figure 3 shows the time paths of the labor share in agriculture for the countries in our sample. The panels group countries with similar experiences. For the U.S., Finland, Sweden, and Japan, our data covers essentially the whole process of structural change, with initial agricultural labor shares in the neighborhood of 80%. For the remaining countries in our sample (UK, Canada, France, Germany, Italy, Belgium, the Netherlands, Spain, and South Korea) the period covered is shorter, but on average our data still captures reallocations that affect more than 25% of the labor force.

As emphasized by the model, the historical evidence suggests that structural change

⁸For some countries where no measure of the price of manufacturing goods is available, we use the GDP deflator relative to the price of agricultural goods. Appendix C shows that this measure changes with changes in relative productivity in the same way as the relative price p does. We focus on manufacturing because this is where resources moved from agriculture. The share of the labor force in services only started to increase when the agricultural share of output was already below 5%, as Buera and Kaboski (2009) show in their work on the U.S. service sector (see their Figure 1).

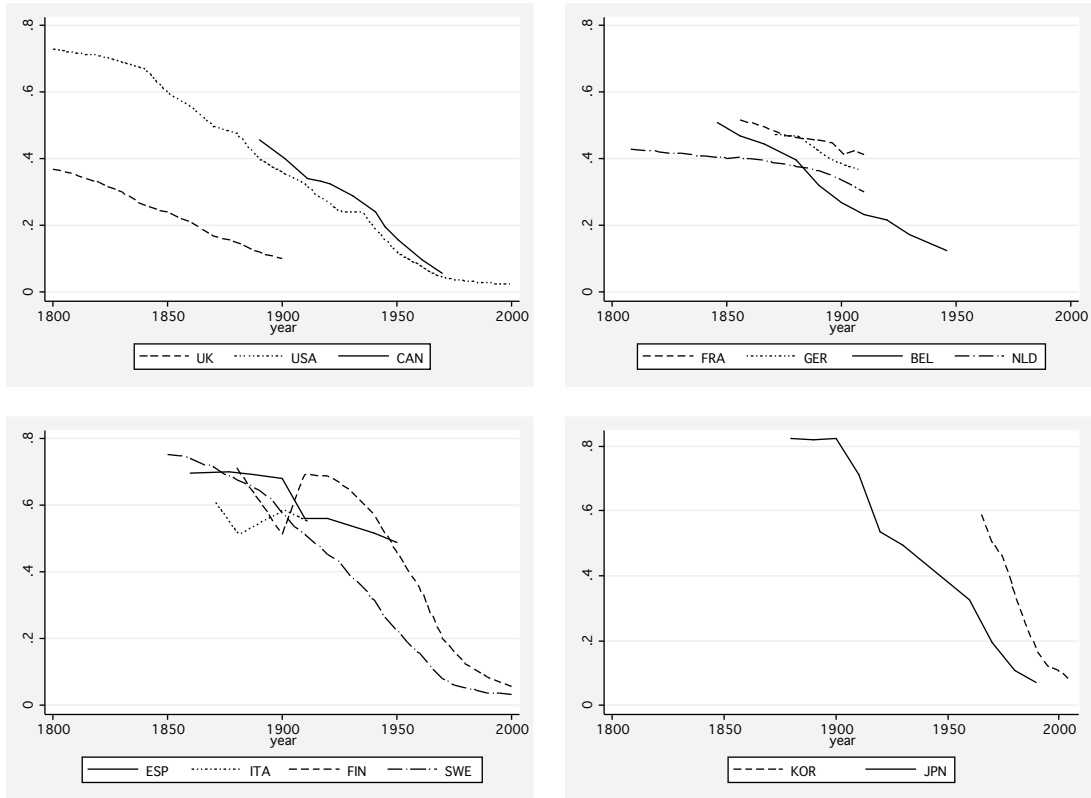


Figure 3: The employment share of agriculture

is a one-way street. Increases in the labor share in agriculture are extremely rare events. Clearly, the UK (top left panel) was the first country to experience substantial structural change, with a labor share in agriculture below 50% as early as 1800. At that time, the U.S. agricultural share was still above 75%. Countries that started the process of structural change later tended to experience a faster pace of migrations. The difference in the speed of change is particularly clear when comparing the European early starters in the top right panel to the European late starters in the bottom left panel. When the latter started their transformations, the former already had very low labor shares in agriculture. Nonetheless, the late starters experienced much faster reallocations and nowadays their agricultural labor shares are not far from those of the earlier starters. The fastest change was experienced by South Korea and Japan.

Similar patterns emerge from the descriptive statistics summarized in Table 1. While

Table 1: Descriptive statistics: structural change

	Average annual change in share of employment in agriculture				
	whole sample	up to 1939	after 1939	after 1939 (countries with pre-1939 data)	while $L^A > 0.1$
mean change (% pts)	-0.434 (0.456)	-0.320 (0.382)	-0.645 (0.508)	-0.530 (0.376)	-0.465 (0.484)
mean rate of change (%)	-1.847 (1.908)	-0.796 (0.803)	-3.788 (1.835)	-3.575 (1.716)	-1.502 (1.723)
fraction < 0	0.959	0.938	1.000	1.000	0.952
observations	148	96	52	44	125
countries	13	12	8	7	13

Notes: Computed using 5-year moving averages of the variables for period where both price and labor share data is available. Standard errors in parentheses. The mean rate of change is the mean annualized % change. The mean change is in percentage points.

the standard deviation in the pooled data is substantial, virtually all episodes consist of migrations out of agriculture. On average over the whole sample, the agricultural labor share has dropped by 0.4 percentage points per year. This translates into a rate of decline of that share of 1.8% per year. At this rate it takes around 60 years to reduce the agricultural labor share from 60%, the average labor share at the beginning of our sample, to 20%. Structural change was slower before World War II (average annual change of -0.3 percentage points or a rate of change of -0.8%) and faster afterwards (-0.6 percentage points or -3.8%). This tendency holds even when we restrict our sample to those industrialized countries for which pre-war data is available.

The first two columns of Table 2 present the average annual change and the average annual growth rate of the labor share in agriculture at the country level. It is clear that the variation across countries is substantial. While part of this is due to differences in data coverage across countries, most of it remains when computing the same statistics for smaller, balanced panels.⁹ As was already evident in Figure 1, the late starters, perhaps

⁹In constructing balanced panels, there is a tradeoff between the number of countries and the overall number of observations that can be included. The most encompassing balanced panels cover seven countries over either 1860 to 1900 or 1890 to 1930. Clearly, the unbalanced panel with its much larger coverage is much more informative. In the 1860-1900 balanced panel, there is about half as much cross-

Table 2: Descriptive statistics for historical data: Structural change and the change in the relative price of manufactures by country

country	dL^A (% pts)	$g(L^A)$ (%)	$g(p)$ (%)	data coverage
Belgium	-0.38	-1.40	-0.26	1846 - 1946
Canada	-0.50	-2.59	-0.10	1890 - 1970
Finland	-0.55	-2.08	-0.22	1880 - 2000
France	-0.20	-0.42	-0.33	1856 - 1911
Germany	-0.29	-0.69	-0.69	1871 - 1907
Italy	-0.14	-0.24	0.34	1871 - 1911
Japan (1880-1930)	-0.66	-1.02	-0.40	1880 - 1930
(1960-1990)	-0.84	-4.88	-2.42	1960 - 1990
Netherlands	-0.14	-0.38	-0.69	1820 - 1910
South Korea	-1.28	-4.84	-3.25	1965 - 2005
Spain	-0.23	-0.40	-0.15	1860 - 1950
Sweden	-0.48	-2.08	0.12	1850 - 2000
UK	-0.29	-1.48	0.20	1820 - 1900
USA	-0.38	-1.85	0.25	1820 - 1999

Notes: Computed using 5-year moving averages of the variables for period where both price and labor share data is available. All changes are annualized. For Japan, there are only two disjoint series for the relative price, so we treat the two periods separately. d denotes a difference, $g(\cdot)$ a growth rate.

with the exception of Spain and Italy, experienced the fastest rates of structural change while France, Germany, Italy and the Netherlands had a much slower, drawn-out process.

4.2 The relative price and structural change

Table 3 shows descriptive statistics for changes in the relative price of manufactures. The average change in the relative price is slightly negative, an average decrease of less than one third of a percentage point per year. Around half of the observations fall on each side of zero, with a substantial standard deviation. For all countries taken together, the relative price declines more quickly after World War II. Here, however, sample composition

country variation in structural change as in the unbalanced one, while in the 1890-1930 one, there is almost as much as in the unbalanced panel.

matters. Considering only those countries for which we also have data for the period before 1939, a pattern similar to that observed in the U.S. emerges: the relative price of manufactures falls before World War II and increases afterwards.

Table 3: Descriptive statistics: the relative price of manufactures

	Annualized % change in the relative price of manufactures				
	whole sample	up to 1939	after 1939	after 1939 (countries with pre-1939 data)	while $L^A > 0.1$
mean rate of change (%)	-0.279 (2.303)	-0.161 (1.692)	-0.498 (3.142)	0.011 (2.921)	-0.595 (2.229)
fraction < 0	0.493	0.510	0.462	0.386	0.552
observations	148	96	52	44	125
countries	13	12	8	7	13

Notes: Computed using 5-year moving averages of the variables for period where both price and labor share data is available. Standard errors in parentheses. The mean rate of change is the mean annualized % change.

In the light of equation (9), the fact that the average change in the relative price is slightly below zero suggests that non-agricultural technological change has outpaced its agricultural counterpart, again echoing the U.S. experience before World War II. It is also obvious from the third column of Table 2 that in Japan and Korea, where the move out of agriculture was particularly fast, the relative price of manufacturing goods plummeted, suggesting that improvements in manufacturing productivity were the main driver of the process there. These conclusions would hold only more strongly if the change in the relative price was overstated due to failure of price indices to account for quality improvements, which arguably are larger for manufactures than for agricultural goods.¹⁰

¹⁰As discussed in footnote 5, the relationship between labor allocations and relative prices (productivities) would be different in an open economy. Nonetheless, there are two reasons that make us believe that the close economy assumption is a reasonable approximation for the countries and periods under consideration. First, trade in agricultural products was very limited. For instance, despite being the main grain exporter in the late 19th century, U.S. grain exports amounted to less than 10% of the quantity produced (*Getreidehandel, -Produktion und -Preise* 1907). Second, relative prices do not co-move very much across countries. While most of the 23 pairwise correlation coefficients for changes in the relative prices that we can compute are positive, only three are statistically significant at the 10% level, and of these only

In order to explore the determinants of structural change more formally, we regress the rate of change in the share of labor in agriculture in each country on the log of the relative price in that country and a country specific intercept. Empirically, this specification is motivated by the fact that we cannot reject that the agricultural share follows a random walk with country-specific drift. Its growth rate and the relative price are stationary.¹¹ Theoretically, the rate of change of the agricultural labor share is a function of the aggregate rate of technological change, which is unobserved, and of its composition, about which the relative price contains information. The country fixed effects capture the average effect of aggregate technological change at the country level. This is important since the evidence presented in Table 2 points to important variations in the speed of structural change across countries. The coefficient on the relative price shows whether the composition of technological change has an effect on the speed of structural change. Finally, given our focus on the process of development, we restrict our analysis to the period where the share of employment in agriculture exceeds one tenth.¹² This approach is preferable to limiting the time period under consideration since it preserves more observations. The resulting regression equation is

$$g(L_{it}^A) = \alpha_i + \beta \ln p_{it} + \epsilon_{it},$$

where we compute the growth rate of the labor share in agriculture as the annualized growth rate between two consecutive observations.

A positive coefficient β in this regression implies that decreases in the relative price are associated with faster than average decreases in the agricultural labor share. A negative coefficient implies that it is increases in the relative price which are associated with faster structural change. It then follows from equation (9) that a positive coefficient indicates that the labor pull channel has a stronger effect on the structural transformation than

two are larger than 0.5. If trade was an important determinant of the relative price (and therefore of the labor allocation) then we would expect much higher price correlations. The low importance of trade in agricultural output is in line with what Gollin, Parente and Rogerson (2007) document for poor countries nowadays.

¹¹We use the panel unit root test recommended by Bond, Nauges and Windmeijer (2005) and Hall and Mairesse (2005), using 10-year lags to maximize the number of observations. Unlike most other panel unit root tests, this one can be applied to our data despite the somewhat irregular structure that is unavoidable when combining historical data across countries. The order of integration of the variables that we find could arise if the productivity of each sector is a random walk. The agricultural share could inherit this property, while the relative price, which depends on the productivity ratio, need not.

¹²This threshold was reached by the UK as soon as 1891, by Canada in 1951, and by the U.S. in 1955.

the labor push channel. As discussed above, a negative coefficient leaves several possible interpretations. While the statistics on changes in the relative price presented in Table 3 contain information on the prevalence and frequency of the two channels, the regression thus captures additional information on their relative strength.

Table 4 presents the basic regression results. The coefficient on the relative price is positive and strongly significant across specifications suggesting that in our sample, the labor pull effect affects the labor allocation more strongly than the labor push effect. In a model with limited labor mobility, labor reallocation would lag behind the relative price adjustment. This scenario is explored in the second column of Table 4, which uses the lagged log relative price as a regressor. The sign, size, and significance of the coefficient are essentially unaffected by this change. The estimates reported in the third column suggest that structural change accelerates as the labor share in agriculture falls – this corresponds to the speeding up of the structural transformation after 1939 that was already visible in the descriptive statistics in Table 1. Still, the sign of the coefficient on the relative price is not affected by the introduction of the lagged agricultural share, suggesting once more that changes in non-agricultural technology have been the main driver behind the process of structural change in our sample.

These results are robust to changes in the specification and in the data selection rules. First, an interaction of the price and the lagged share is not significant. (Results not reported.) A quantile regression with the same specification as column 1 also yields estimates that barely change across quantiles of the dependent variable. Hence, the “pull” channel has a stronger effect on the labor share at all stages of the structural transformation. Results are also robust to the exclusion of individual countries, or to setting the agricultural share threshold for inclusion in the sample at 5% or at 15% (instead of 10%).¹³

The evidence reported in this section suggests that labor pull – increases in non-agricultural technology – has been the main driver behind the large migrations out of the agricultural sector that began more than two centuries ago in the UK. First, since the average change in the relative price in our sample is slightly negative, equation (9)

¹³An interaction of the relative price with a dummy indicating whether the price is measured as p_m/p_a or as p_y/p_a is not significant. Nor do results change when splitting the sample along these lines, with the exception of the relative price losing significance in the column 3 specification if the price is measured as p_y/p_a . This is not surprising as the split samples are much smaller.

Table 4: Regression results: the relative price and changes in the fraction of employment in agriculture

	Dependent variable: $g(L^A)$		
	(1)	(2)	(3)
$\ln p_t^i$	0.034 *** (0.008)		0.014 ** (0.006)
$\ln p_{t-10}^i$		0.025 *** (0.007)	
lagged share of agriculture			0.053 *** (0.010)
constant	-0.018 *** (0.001)	-0.019 *** (0.001)	-0.040 *** (0.004)
R^2	0.203	0.120	0.393
observations	125	107	107
countries	13	12	12

Notes: The dependent variable is the growth rate of the labor share in agriculture (average yearly growth rate between an observation and the previous observation). Variables are 5-year moving averages if data is at a higher frequency. Only observations where the labor share in agriculture is at least 10% are included. The regression includes country fixed effects. Robust standard errors (clustered at country level) in parentheses. Stars indicate statistical significance at the 90% (*), 95 (**) and 99% (***) level, respectively. Lagged share of agriculture refers to a ten-year lag.

implies that non-agricultural technological change has marginally outpaced its agricultural counterpart. Second, our regression analysis complements this result, suggesting that in pull episodes, labor reallocation occurred at a faster pace than in labor push episodes.

Our results have important implications for modeling the process of structural change. On the one hand, models of structural change that rely on faster productivity growth in agriculture, such as Ngai and Pissarides (2007), seem to be at odds with most of the the pre-World War II evidence. On the other hand, models of structural change that restrict non-homotheticities in preferences to food consumption, such as Gollin et al. (2002), seem to miss non-agricultural technological progress as an important driver of structural change. Finally, our results cast some doubts on some of the policy recommendations derived using modeling strategies that neglect the crucial role played by non-agricultural productivity in the process of structural change and economic development.

5 Conclusions

Recent years have seen a renewed interest in the role of agriculture in the process of development and structural change, motivated by the large role agriculture still plays in today's poor economies and by its importance for their aggregate productivity. Yet, there has been and still is a substantial debate about the relative roles played by agricultural and non-agricultural productivity in the structural transformation out of agriculture. The goal of this paper was to shed some light on this debate by examining the experience of countries that completed this transformation.

We presented a simple model consistent with the two crucial observations associated with the process of structural change: a secular decline in the share of the labor force devoted to agriculture and a decreasing weight of agricultural output in national product. We used this framework to explore the theoretical implications of the “labor push” and “labor pull” hypotheses that point to technological progress in agriculture and manufacturing, respectively, as the main driver of structural change. Then, using two data sets covering the structural transformation of 13 countries that completed that process, we explored the relative contribution of the two channels to the process of structural change.

This analysis yielded three main results. Firstly, both channels matter. In the case of the U.S., for instance, the “labor pull” channel dominated before World War I, with the “labor push” channel taking over after World War II. Secondly, on average, increases in non-agricultural productivity played a slightly larger role than those in agricultural productivity, pointing to the “labor pull” channel as a somewhat more important engine of structural change overall. Finally, we found that the agricultural labor share declined more when the productivity of manufacturing increased relative to that of agriculture. Overall, while the “labor push” channel matters at times, this evidence indicates that the “labor pull” channel was the main engine behind the massive reallocations of labor out of agriculture that began in the UK more than two centuries ago.

Our results are a crucial input for the growing theoretical work on structural change and may have important implications for the understanding and design of adequate development policies.

Appendix

A Basic results under CES preferences

Assume preferences of our representative household are given by,

$$U(c_t^A, c_t^M) = \left[(1 - \eta)^{\frac{1}{\nu}} (c_t^A - \gamma)^{\frac{\nu-1}{\nu}} + \eta^{\frac{1}{\nu}} (c_t^M)^{\frac{\nu-1}{\nu}} \right]^{\frac{\nu}{1-\nu}}, \quad \alpha, \mu > 0; \nu > 0,$$

where c_t^A and c_t^M denote individual consumption of food and non-agricultural goods respectively, η is the relative weight of non-agricultural goods in preferences and ν is the elasticity of substitution between the two types of goods. Under this preference specification (6) becomes

$$\frac{\gamma}{A} = G(1 - L_t^M) - \frac{1 - \eta}{\eta} \left(\frac{A}{M} \right)^{\nu-1} \left[\frac{G'(1 - L_t^M)}{F'(L_t^M)} \right]^{\nu} F(L_t^M) \equiv \phi^{CES}(L_t^M, M, A), \quad (10)$$

with

$$\phi^{CES}(1, \bar{M}, \bar{A}) < \phi^{CES}(0, \bar{M}, \bar{A}) = G(1); \quad \phi_{L_t^M} < 0. \quad (11)$$

On the one hand, the labor pull hypothesis requires $\phi_M^{CES} > 0$ which implies that the elasticity of substitution has to exceed unity, $\nu > 1$. On the other hand, since $\text{sign}(\phi_M^{CES}) = -\text{sign}(\phi_A^{CES})$, the labor push hypothesis requires that $\nu > 1$ is not too large.¹⁴ If these two restrictions on the degree of substitutability between agricultural and non-agricultural goods hold, then all the results presented in Section 2 are valid under this preference specification that abstracts from μ . In addition, as in Ngai and Pissarides (2007) differential productivity growth across sectors results in structural change even when the last source of non-homotheticity, $\gamma = 0$, is removed.¹⁵ The intuition for this result is as follows. If the elasticity of substitution ν is above 1, an increase in M reduces the price of the non-agricultural good, and since both goods are good substitutes, induces a more than proportional increase in its demand that leads to a reallocation of labor to the non-agricultural sector. An increase in agricultural productivity reduces the price

¹⁴Specifically, we need $\gamma - \frac{1 - \eta}{\eta}(\nu - 1) \left[\frac{AG'(1 - L_t^M)}{MF'(L_t^M)} \right]^{\nu} MF(L_t^M) > 0$ This inequality holds for sufficiently small values of $\nu > 1$.

¹⁵Nonetheless, when $\gamma = 0$, only the labor pull hypothesis would be consistent with the path of migrations observed in the data. This is because our restrictions on ν imply that an increase in agricultural productivity leads to an increase in the share of labor employed in this sector.

of food, causing opposing income and substitution effects. The substitution effect tends to raise food demand, while the income effect implies a reduced food expenditure share because the income elasticity of food is less than one. Our second restriction on the size of v ensures that the income effect dominates the substitution effect and therefore an increase in A is associated with a reduction in the agricultural labor force.

B Data sources

See Tables 5 and 6.

Table 5: Historical data: sources and definitions

country	Share of employment in agriculture	Relative price
Belgium	Mitchell (2003, Table B1)	Price indices for agricultural output and for total output, imputed from the Groningen Growth and Development Centre Historical National Accounts Database (Smits, Woltjer and Ma 2009), which for Belgium mainly draws on Horlings (1996)
Canada	Historical Statistics of Canada series #D1_7	General Wholesale Price Index, Fully and chiefly manufactured, and Wholesale Price Index of Canadian farm products, Statistics Canada ^a
Finland	Mitchell (2003, Table B1)	Price indices for agricultural output and for total output, imputed from the Groningen Growth and Development Centre Historical National Accounts Database (Smits et al. 2009), which for Finland draws on Hjerppe (1989, 1996)
France	Mitchell (2003, Table B1)	Price indices for agricultural output and for total output, imputed from the Groningen Growth and Development Centre Historical National Accounts Database (Smits et al. 2009), which for France draws on Toutain (1987)
Germany	1871: <i>Statistisches Jahrbuch für das Deutsche Reich</i> (1974 [1880]), 1882-1939: Mitchell (2003, Table B1)	Wholesale price indices for agriculture and manufacturing, Jacobs and Richter (1935)

^aFarm products index constructed by linking two indices (1890-1934 and 1926-1970).

country	Share of employment in agriculture	Relative price
Italy	Mitchell (2003, Table B1)	Wholesale price index and Bread and Flour price index, Fenoaltea (2002, Table A.1)
Japan	Mitchell (1998)	1874-1939: Price index of agricultural products and of manufacturing, <i>Choki Keizai Tokei (Estimates of Long-Term Economic Statistics of Japan Since 1868)</i> (1967); ^a 1960-1980: Domestic Corporate Goods Price Index and Agricultural Price Index, Statistics Bureau ^b
Netherlands	Smits, Horlings and van Zanden (2000)	Price indices for agricultural output and for total output, imputed from the Groningen Growth and Development Centre Historical National Accounts Database (Smits et al. 2009), which for the Netherlands draws on various sources, in particular Smits et al. (2000)
South Korea	Mitchell (1998)	Producer price indices for agriculture and manufacturing, South Korean National Agricultural Cooperative Federation ^c
Spain	Mitchell (2003, Table B1)	Price indices for agricultural output and for total output, imputed from the Groningen Growth and Development Centre Historical National Accounts Database (Smits et al. 2009), which for Spain draws on Prados de la Escosura (2003)
Sweden	Data compiled by Rodney Edvinsson, Stockholm University, www.historicalstatistics.org	Price indices for agricultural output and for total output, imputed from Swedish Historical National Accounts, compiled by Olle Krantz and Lennart Schön, available in Lund University Macroeconomic and Demographic Database http://www.ehl.lu.se/database/LU-MADD/National%20Accounts/default.htm
UK	Clark (2002, Table 3)	Price indices for Principal Industrial Products and for Agricultural Products, Mitchell (1988)
USA	1800-1900: Weiss (1992, 1993), 1910-2000: U.S. Department of Commerce (1975, series D5 and D6); Dennis and Iscan (2009)	1800-1913: Wholesale price indices for all commodities and for farm products (series E52 and E53), U.S. Department of Commerce (1975, Warren and Pearson series), Hanes (1998); ^d 1913-1954: Wholesale price indices for industrial commodities and for farm goods, U.S. Department of Commerce (1975, series E23, E25); 1954-2001: Producer price indices for farm products and industrial commodities, Council of Economic Advisers (2002, Table B-67); Dennis and Iscan (2009)

^aPages 165, 195, 197, 200, 203, 207.

^bStatistical Survey Department, Statistics Bureau, Ministry of Internal Affairs and Communications. Tables 22-1 and 22-10. Downloaded from <http://www.stat.go.jp/english/data/chouki/index.htm>.

^cData downloaded from <http://kosis.nso.go.kr>.

^dHanes extended the series to 1860-1990 using the same method underlying the Warren and Pearson indices.

Table 6: Data coverage

country	share of employment in agriculture		relative price	
	period	observations	period	observations
Belgium	1846 - 1946	10	1835 - 1953	107
Canada	1881 - 1970	12	1890 - 1970	81
Finland	1880 - 2000	12	1860 - 2001	142
France	1856 - 1936	11	1815 - 1938	118
Germany	1871 - 1939	7	1792 - 1913	122
Italy	1871 - 1971	10	1861 - 1914	54
Japan	1872 - 1990	14	1874 - 2004	59
Netherlands	1800 - 1913	114	1807 - 1939	121
South Korea	1955 - 2006	46	1965 - 2006	42
Spain	1860 - 2001	13	1850 - 1958	109
Sweden	1850 - 2000	151	1800 - 2000	201
UK	1800 - 1930	14	1800 - 1900	101
USA	1800 - 2000	103	1800 - 2000	201

C The measure of the manufacturing price

For some countries where no measure of the price of manufacturing goods is available, we use the GDP deflator relative to the price of agricultural goods. This Appendix shows that this measure changes with changes in relative productivity of the two sectors in the same way as the ideal relative price would.

For this, first derive the correct consumption-based aggregate price index. With non-homothetic preferences, this requires some precision because the marginal expenditure needed to raise by one unit is not constant and therefore does not coincide with the average expenditure per unit of utility. (This distinguishes this setup from e.g. a setup with Dixit-Stiglitz preferences, where such a consumption-based price index is often used, and where the two concepts coincide.)

Let P be the marginal expenditure needed to raise utility by one unit beyond \bar{u} and

\bar{P} the minimum expenditure needed to reach utility \bar{u} . \bar{P} solves the problem

$$\begin{aligned} \min_{c_a, c_m} & p_a c_a + p_m c_m \\ \text{s.t.} & \beta \ln(c_a - \gamma) + \ln(c_m + \mu) = \bar{u}. \end{aligned}$$

P is the multiplier on the constraint. The first order conditions are

$$\begin{aligned} p_m &= \frac{P}{c_m + \mu} \\ p_a &= \frac{\beta P}{c_a - \gamma}. \end{aligned} \tag{12}$$

Plugging this into the constraint and solving for P yields

$$P = \beta^{-\frac{\beta}{1+\beta}} [\exp(\bar{u})]^{\frac{1}{1+\beta}} p_m^{\frac{1}{1+\beta}} p_a^{\frac{\beta}{1+\beta}}.$$

Using this,

$$\frac{P}{p_a} = \beta^{-\frac{\beta}{1+\beta}} [\exp(\bar{u})]^{\frac{1}{1+\beta}} \left(\frac{p_m}{p_a} \right)^{\frac{1}{1+\beta}}. \tag{13}$$

Clearly, $\ln(P/p_a)$ varies proportionally with $\ln(p_m/p_a)$.

Obtain \bar{P} by evaluating the objective function at the optimum:

$$\begin{aligned} \bar{P} &= p_m c_m + p_a c_a = (1 + \beta)P - p_m \mu + p_a \gamma \\ &= (1 + \beta) \beta^{-\frac{\beta}{1+\beta}} [\exp(\bar{u})]^{\frac{1}{1+\beta}} p_m^{\frac{1}{1+\beta}} p_a^{\frac{\beta}{1+\beta}} - p_m \mu + p_a \gamma \\ \frac{\bar{P}}{p_a} &= (1 + \beta) \beta^{-\frac{\beta}{1+\beta}} [\exp(\bar{u})]^{\frac{1}{1+\beta}} \left(\frac{p_m}{p_a} \right)^{\frac{1}{1+\beta}} - \frac{p_m}{p_a} \mu + \gamma \end{aligned} \tag{14}$$

Then

$$\frac{\partial(\bar{P}/p_a)}{\partial(p_m/p_a)} = \beta^{-\frac{\beta}{1+\beta}} \left[\left(\frac{\beta P}{p_a} \right)^{\beta} \frac{P}{p_m} \right]^{\frac{1}{1+\beta}} \left(\frac{p_m}{p_a} \right)^{\frac{1}{1+\beta}-1} - \mu = \frac{P}{p_m} - \mu = c_m,$$

which is strictly positive for all countries in the data.

Hence, p_y/p_a moves in the same direction as p_m/p_a no matter whether the historical price indices we use measure average or marginal expenditure. As a result, while it is not legitimate to compare levels of indices between countries using p_m vs p_y , within-country changes in the relative price reflect changes in p_m/p_a , and thus changes in the sectoral productivities, no matter whether they are measured using p_m or p_y .

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